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## Recording site dependence of the neuronal spiking statistics

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### Abstract

Spiking characteristics of neurons in the middle temporal (MT) area and the medial superior temporal (MST) area in the visual cortex of a monkey are compared with the ones in the principal sulcus (PS) area in the prefrontal cortex. The comparison is based on the basis of three inter-spike interval statistical measures: the coefficient of variation (CV), the skewness coefficient (SK) and the correlation coefficient of consecutive intervals (COR). Even for the spike sequences recorded from the same neuron, three coefficients computed from 100 intervals do not always exhibit similar values, but distribute rather widely. The distribution of three coefficients obtained from a single neuron in the MST area does not largely deviate from the distribution obtained from multiple neurons in MT and MST areas. Those distributions, however, largely deviate from the distribution obtained from neurons in the PS area. In this way, the distribution of those statistical coefficients reflects the nature of the recording site. © 2002 Published by Elsevier Science Ireland Ltd.

**Keywords:** Coefficient of variation; Skewness coefficient; Correlation coefficient; Cortical area

### 1. Introduction

The cerebral cortex is divided into discrete areas on the cytoarchitectural basis. The cytoarchitecturally divided areas turned out to have distinct physiological functions. In addition to the difference in cytoarchitectures and the physiological functions, neurons in different cortical areas may exhibit different spiking characteristics. The difference may even be seen in gross spike rate. For instance, when a visual flow to some direction is

shown to a monkey, neurons in the middle temporal (MT) and the medial superior temporal (MST) areas in the visual cortex can exhibit high spike rate, of several tens of spikes per second, or even higher. On the other hand, neurons in the prefrontal cortex do not exhibit such high spike rate, in response to external stimuli as well as internal memory contents. Therefore, if we are to attempt to infer the source of the spike train received, the gross spike rate may become a clue to the inference. In the present paper, we are concerned with higher order non-dimensional statistical measures such as the coefficient of variation (CV), the skewness coefficient (SK), and the correlation coefficient of consecutive intervals (COR) to see if they may supply firmer clues to that inference of the recording site.

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51 We analyzed the spike sequences recorded from  
52 the distinct areas: the MT and the MST areas in  
53 the visual cortex and the principal sulcus (PS) area  
54 in the prefrontal cortex. It is found that the  
55 distributions of the non-dimensional statistical  
56 measures evaluated from the recorded data are  
57 largely dependent on the recording site.

## 58 2. Materials and method

59 The spiking characteristics may depend not only  
60 on the recording site, but also on the animal's  
61 behavioral conditions. In order to extract the  
62 recording site dependence of the spiking charac-  
63 teristics from multiple experiments, other condi-  
64 tions have to be made as similar as possible. For  
65 this reason we required the experiments using same  
66 kind of animals. All the following experiments are  
67 performed by using macaque monkeys. We also  
68 require the animals to take behaviorally steady  
69 condition. The first two experiments are per-  
70 formed using an anesthetized monkey, and the  
71 steady conditions are naturally satisfied. The third  
72 experiment used awake, behaving monkeys but the  
73 spiking data, which are used for the analysis, are  
74 taken from the period in which the monkey is  
75 staying still, as explained later.

76 1) 'MT/MST'(experiment carried out by Hiroshi  
77 Ohno, Tamagawa University): computer gen-  
78 erated random dots uniformly moving to a  
79 fixed direction were shown to an anesthetized  
80 macaque monkey whose eyes are still. Spike  
81 sequences were recorded from multiple neu-  
82 rons sampled from the MT and the MST  
83 areas, which are known to exhibit selective  
84 response to motion of visual objects. Record-  
85 ing neuronal activities was carried out with the  
86 standard single extracellular recording  
87 method. Twelve directions of motion mutually  
88 different with 30 degree in angle were tested  
89 with respect to a single neuron. Moving  
90 random dots to one direction are shown for  
91 10 s, respectively. It is known that the  
92 response latency of this area is less than 50  
93 ms (see [Kawano et al., 1994](#)). From each 10-s  
94 record, the initial 0.5 s is removed from

analysis, regarding those 500 ms as initial  
transients. If the spike sequence of the remain-  
ing 9.5 s contain more than 100 intervals, we  
take the central 100 intervals to compute the  
three statistical coefficients CV, SK and COR.  
The spike records, which do not contain 100  
intervals, are dismissed. About 20 neurons  
sampled from the MT and the MST areas  
were recorded and we obtained 73 spike  
sequences with 100 intervals, which were  
subsequently used to compute the statistical  
coefficients.

2) 'MST-1' (experiment carried out by Hiroshi  
Ohno, Tamagawa University): spike se-  
quences were recorded from a single neuron  
in the MST area of a macaque monkey.  
Experimental circumstances are same as  
above. The direction of random dots is chosen  
so as to result the largest response of the  
neuron (so called preferred direction). The  
optimal visual flow is shown for a period of 5 s  
repeatedly (97 times) with rest intervals of a  
several seconds. From each spike record, we  
also removed the initial 0.5 s, regarding the  
period as initial transient. We linked the  
multiple spike records according to the pre-  
scription, which we called 'L1' in [Shinomoto  
et al. \(1999\)](#), [Sakai et al. \(1999\)](#). That is to link  
the segments of different trials directly. We  
keep the last fragmental interval of one 4.5-s  
segment and the first fragmental interval of  
the next 4.5-s segment to compose one inter-  
val. From the long sequence, made up by  
linking the records, spike sequences of 100  
intervals are taken out one by one. Eventually  
we got 55 spike sequences of 100 intervals,  
from each of which we compute a set of the  
three statistical coefficients.

3) 'PS' (by courtesy of Shintaro Funahashi,  
Kyoto University): spike sequences are re-  
corded from multiple neurons sampled from  
the PS area of alert macaque monkeys per-  
forming a delay response task of [Funahashi  
and Inoue \(2000\)](#). Recording neuronal activ-  
ities was carried out with the standard extra-  
cellular recording method. Recorded spike  
rate of a prefrontal cortical neuron is found  
typically ten spikes per s. The behavioral

143 steady state we could obtain in this case is the  
 144 delay period of 3 s in a delay response task, in  
 145 which a monkey is required to keep the cue  
 146 memory, which is necessary for the correct  
 147 delayed response. From those 3 s, the initial  
 148 and final 0.5 s are removed as transients and  
 149 the spike sequence left for analysis is only 2 s.  
 150 As the number of intervals obtained from this  
 151 fragment of time does not serve 100, we linked  
 152 the records of different trials of the same cue  
 153 stimulus by the method of linkage L1 ex-  
 154 plained above, by assuming that the neuron  
 155 has been subject to the same statistical condi-  
 156 tion when the monkey was exposed to the  
 157 same cue information. About 233 neurons in  
 158 the PS area were recorded and we obtained  
 159 666 spike sequences with 100 intervals.

### 160 3. Three statistical coefficients

161 In comparing characteristics of multiple spike  
 162 sequences, it is desirable to standardize the length  
 163 of the spiking data. We fix the number of intervals  
 164 to 100. From the sequence of 100 intervals  $\{T_1, T_2,$   
 165  $\dots, T_{100}\}$  prepared accordingly, we compute three  
 166 statistical coefficients: the CV, the SK, and the  
 167 COR, respectively, defined below.

168 The CV is a measure of randomness defined as  
 169 the ratio of the standard deviation to the mean,

$$170 \text{ CV} = \frac{\overline{(T - \bar{T})^2}^{1/2}}{\bar{T}}, \quad (1)$$

171 where and hereafter  $\overline{\quad}$  represents an averaging  
 172 operation over the number of intervals, such that  
 $\bar{T} = 1/n \sum_{i=1}^n T_i$ .

173 The SK is a coefficient of the asymmetry of the  
 174 interval distribution, defined as

$$175 \text{ SK} = \frac{\overline{(T - \bar{T})^3}}{\overline{(T - \bar{T})^2}^{3/2}}. \quad (2)$$

176 The COR is a coefficient of mutual dependence  
 of consecutive interspike intervals, defined as

$$177 \text{ COR} = \frac{\overline{(T_i T_{i+1} - \bar{T}^2)}}{\overline{(T - \bar{T})^2}}, \quad (3)$$

where,  $T_i$  and  $T_{i+1}$  denote a pair of the con-  
 secutive intervals.

### 4. Two-sample test

180 Fig. 1 depicts distributions of three statistical  
 181 measures CV, SK and COR, computed from the  
 182 above-mentioned three kinds of spike data sets.  
 183 Fig. 2 depicts the corresponding normalized histo-  
 184 grams. In order to quantify the statistical signifi-  
 185 cance of the mutual difference of those  
 186 distributions, we employ here the two-sample  
 187 test, which measures the sample mean difference.  
 188 The  $t$  measure for the two-sample test is given by

$$189 t = \frac{\bar{x}_A - \bar{x}_B}{s} \sqrt{\frac{n_A n_B}{n_A + n_B}}, \quad (4)$$

where  $x_A$  or  $x_B$  stand for the statistical measures  
 computed for the respective two groups A and B,  
 $n_A$  and  $n_B$  are the number of ISI sequences of 100  
 intervals and

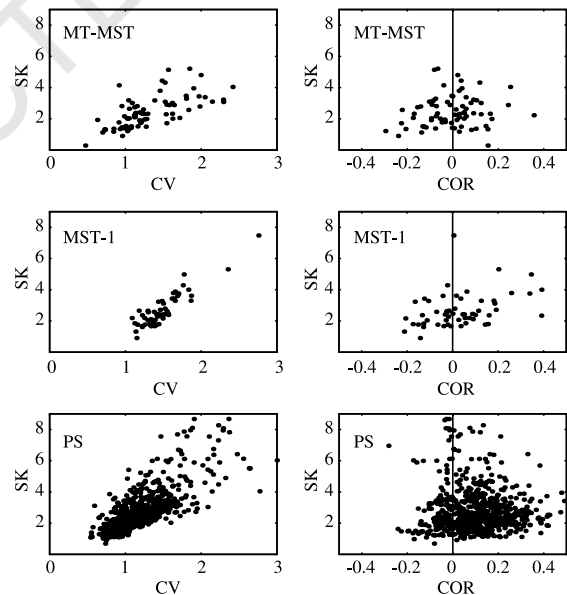


Fig. 1. Distribution of (CV, SK) and (COR, SK) values, respectively, taken from MT/MST, MST-1 and PS. Each dot represents the pair of statistics computed from 100 ISIs.

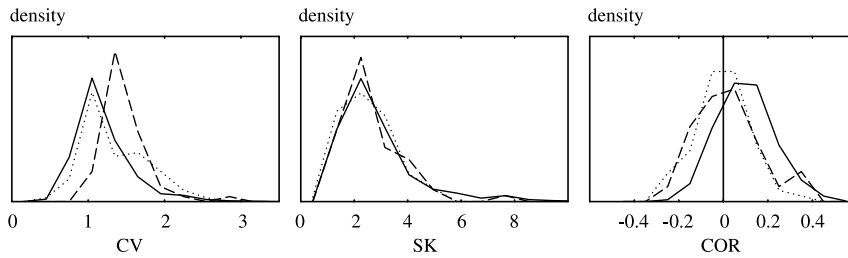


Fig. 2. Normalized histograms of three statistical measures CV, SK, and COR. Histograms of the spike data sets 1 (PS), 2 (MST-1) and 3 (MT/MST) are, respectively, shown in the solid line, broken line and dotted line.

$$193 \quad \bar{x}_A = \frac{1}{n_A} \sum_{i=1}^{n_A} x_A^i, \quad (5)$$

$$194 \quad \bar{x}_B = \frac{1}{n_B} \sum_{j=1}^{n_B} x_B^j, \quad (6)$$

$$195 \quad s^2 = \frac{\sum_{i=1}^{n_A} (x_A^i - \bar{x}_A)^2 + \sum_{j=1}^{n_B} (x_B^j - \bar{x}_B)^2}{n_A + n_B - 2}. \quad (7)$$

196 If two data sets are drawn from the same  
 197 distribution, this  $t$  measure is expected to obey  
 198 Student's  $t$ -distribution of the degree of freedom  
 199  $n_A + n_B - 2$ . In any pair of the data sets MT/MST,  
 200 MST-1 and PS, the degree of freedom  $n_A + n_B - 2$   
 201 is larger than 100. In such a large degree of  
 202 freedom, the  $t$ -distribution is close to the standard  
 203 normal distribution  $N[0, 1]$ . Table 1 summarizes  
 204 the  $t$  values with respect to the statistical measures,  
 205 CV, SK and COR, evaluated for all pairs chosen  
 206 from the three kinds of data sets MT/MST, MST-1  
 207 and PS. Those  $t$  values should be compared with  
 208 reference two-sided percentiles:  $t = 1.7, 2.6,$  and  
 3.3, respectively, for 10, 1 and 0.1%.

Table 1

The  $t$ -values with respect to CV, SK and COR evaluated for all pairs chosen from the three kinds of data set, MT/MST, MST-1 and PS

	CV	SK	COR
MT-MST vs. MST-1	2.40	1.20	1.61
MT-MST vs. PS	1.98	1.91	6.86
MST-1 vs. PS	4.42	0.54	3.81

For  $t$ -distribution with the degree of freedom larger than 100, two-sided percentiles for 10, 1, and 0.1% are, respectively,  $t = 1.7, 2.6$  and 3.3.

## 5. Discussion

210 By considering the  $t$  measures of entire three  
 211 statistics, the pairs (MT/MST and PS) and (MST-1  
 212 and PS) can hardly be considered as drawn from a  
 213 single population. In other words, PS is clearly  
 214 distinct from either MT/MST or MST-1. In this  
 215 way the spiking characteristics measured on the  
 216 basis of CV, SK and COR reflect the nature of the  
 217 recording site. The major cause of the difference is  
 218 that the PS neurons exhibited large positive COR  
 219 values in comparison with those of the other two  
 220 areas. The positive COR is considered to reflect  
 221 the slow modulation of the spike rate (see [Shino-](#)  
 222 [moto and Tsubo, 2001](#)). In addition to this, it is  
 223 interesting to see that mean CV values of MT/  
 224 MST and MST-1 are larger than that of PS.  
 225 Neurons in the MT and the MST areas exhibited  
 226 higher spike rate than that of the PS areas. Though  
 227 smaller CV values are naturally expected for  
 228 higher spike rate, the result turned out to be  
 229 opposite. This interesting result may reflect the  
 230 intrinsic nature of the neurons, which constitute  
 231 each area: difference of the neuronal characteris-  
 232 tics or difference in their circumstances.

233 MT/MST and MST-1 are barely considered as  
 234 drawn from the same population. The major cause  
 235 of the difference is due to the deviation of mean  
 236 CV values. But they are relatively similar with each  
 237 other in comparison with the other pairs (MT/  
 238 MST and PS) and (MST-1 and PS). This fact  
 239 implies that a single neuron may represent the  
 240 ensemble characteristics of the area, which should  
 241 be determined from spike sequences of a number  
 242 of neurons in the same area. In this neuron's case,  
 243 we can conclude that the MST-1 statistics are

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244 definitely different from the ensemble statistics of  
 245 the PS area. The problem of whether the single  
 246 neuron spiking statistics represent the ensemble  
 247 spiking statistics should be examined thoroughly  
 248 by obtaining more sequences of multiple neurons.

249 The spiking characteristics may depend not only  
 250 on the recording site, but also on the tasks  
 251 performed, and also individual animals. In order  
 252 to extract the recording site dependence of the  
 253 spiking characteristics from multiple experiments,  
 254 we sought the data whose experimental conditions  
 255 are mutually similar. The points in common are  
 256 the fact that the subject animals are same macaque  
 257 monkeys and animals were in behaviorally sta-  
 258 tionary during recording. The major difference  
 259 would be that the monkey is anesthetized in  
 260 experiment 1 and 2 while the monkeys are alert  
 261 in experiment 3. In order to determine what is the  
 262 essential cause of the difference of spiking char-  
 263 acteristics observed here, we have to lead a new  
 264 experiment in which different areas are recorded  
 265 from a single animal, which is repeating the same  
 266 task.

## 267 6. Uncited reference

268 [Ohno, 2002.](#)

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